

# Evaluating Carbon Capture and Storage in a Climate Model with Directed Technical Change\*

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## Abstract

Carbon capture and storage (CCS) is considered a critical technology needed to curb CO<sub>2</sub> emissions and is envisioned by the International Energy Agency (IEA) as an integral part of least-cost greenhouse gas mitigation policy. In this paper, we assess the extent to which CCS and R&D in CCS technology are indeed part of a socially efficient solution to the problem of climate change. For this purpose, we extend the intertemporal model of climate and directed technical change developed by Acemoglu et al. (2012, *American Economic Review*, 102(1): 131–66) to include a sector responsible for CCS. Surprisingly, we find that even for an optimistic cost estimate available for CCS (\$58/ton of CO<sub>2</sub> avoided) it is not optimal to deploy CCS or devote resources to R&D in CCS technology either in the near or distant future. Indeed, it is only when the marginal cost of CCS is less than \$25/ton that a scenario with an active CCS sector (including R&D) becomes optimal, though not in the near future.

JEL codes: H23,O31,Q43,Q54,Q55

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# 1 Introduction

In 2010, fossil fuels represented more than 80% of global energy use<sup>1</sup> and are responsible for 65% of global anthropogenic greenhouse gas (GHG) emissions (IEA, 2011, pp. 18–19). Although renewables have significant potential in energy production, fossil fuels are expected to remain the dominant source of energy for decades to come.<sup>2</sup> Without specific actions, atmospheric CO<sub>2</sub> concentration will continue to grow and this may prove disastrous for future generations (UNEP, 2006).

Three main policies have been proposed as possible solutions to the problem of climate change: the more intensive use of renewable and nuclear energy; the more efficient generation of power and end-use of energy carriers; and the development and deployment of technologies to capture and store carbon emissions from fossil fuel use.<sup>3</sup> Carbon capture and storage (CCS) technology can be used by large stationary point sources such as fossil fuel-fired power plants and emission-intensive industrial facilities. Its main purpose is to prevent CO<sub>2</sub> emissions from entering the atmosphere. The rates of carbon captured can be as high as 85–95%, in both the pre- and post-combustion systems.<sup>4</sup>

The development of CCS technologies has been advocated by both national governments and international organizations. For example, some high-income oil- and gas-producing countries in Europe and North America are strongly committed to the use of resources in the research, development and demonstration (RD&D) of CCS technologies. Using cross-sectional analysis of OECD countries, Tjernshaugen (2008) finds that fossil fuel reserves and extraction activities are the main variables explaining funding levels for RD&D on CCS. Outstanding examples are Canada and Norway.<sup>5</sup> To give an idea of the orders of magnitude, Tjernshaugen (2008) reports that for these countries the 2005 RD&D budget for CCS normalized by 2002 total government energy-related RD&D expenditures amounted to 6.2% and 38.8% of the total, respectively. The share of Norwegian CCS RD&D clearly stands out. There are two main reasons for why a relatively small country is so concerned with CCS technology. First, with hydropower being historically the main energy carrier in Norway, power generation from fossil fuels was almost absent. When gas-fired power plants were added to the Norwegian energy grid, compliance with domestic emissions targets especially was required, thereby promoting

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<sup>1</sup>Fossil fuels, renewables, and nuclear electric power respectively account for 83%, 8.3%, and 8.7% of total global energy use (EIA, 2011a, Table 1.1).

<sup>2</sup>According to the U.S. Energy Information Administration, fossil fuels will account for 78% of world energy use in 2035 (EIA, 2011b).

<sup>3</sup>The availability of CCS technology also has important implications for bio-energy with CCS, which can offer the prospect of energy supply with large-scale net negative emissions when achieving 2°C target (IPCC, 2014). Another possible policy solution entering recent debate is geoengineering, the intentional, large-scale manipulation of the earth's climate system. See Rasch et al. (2008), Cicerone (2006), and Barrett (2008).

<sup>4</sup>There are three methods for capturing CO<sub>2</sub>. *Post-combustion* carbon capture removes carbon from coal fired power generation or natural gas combined cycles after combustion. Here, CO<sub>2</sub> is separated from the flue gases (whose main constituent is nitrogen) using a liquid solvent. In *pre-combustion* carbon capture, fuel is pretreated and converted into a mix of CO<sub>2</sub> and hydrogen. The hydrogen is then separated from the carbon before being burned to produce electricity. In the *oxy-fuel combustion process*, the fuel is burned using oxygen rather than air. The result is a flue stream of CO<sub>2</sub> and water vapour. Because no nitrogen is present, CO<sub>2</sub> can be easily removed (Golombek et al., 2011; Metz et al., 2005).

<sup>5</sup>In Norway, Technology Centre Mongstad is the world's largest facility for testing and improving CO<sub>2</sub> capture technologies. In Canada, the Boundary Dam Integrated CCS facility started capturing and storing carbon in October, 2014.

the interest in CSS technology and its potential. The second reason is the large contribution of the oil and gas extraction industry to Norway's GDP. The only way to reconcile a strong commitment to environmental policies alongside Norway being a large exporter of fossil fuels is by producing and making available the know-how to prevent the CO<sub>2</sub> generated by burning fossil fuels entering the environment (Tjernshaugen, 2011).

Several international and intergovernmental agencies, including the International Energy Agency (IEA), the Intergovernmental Panel on Climate Change (IIPC), and the U.S. Energy Information Administration (EIA), also envision an important role for CCS as part of an environmentally sustainable global energy policy, and therefore point to the need for significant R&D efforts today in order to endow the world with an economic carbon capturing and storage technology. For example, in IPCC (2005, p. 12), CCS is shown to have the potential to provide 15% to 55% of the world's cumulative GHG mitigation efforts up to 2100. Further, to bring down GHG emissions to 50% of their 2005 level by 2050, IEA (2008) shows that about 27% of the reductions should come from the extensive use of renewables and nuclear energy, 54% from efficiency enhancement, and 19% from CCS activities. Without access to CCS technology, the same report estimates that the overall cost to achieve these emission reductions increases by 70%. In another report, IEA (2009) sketches a road map for CCS and shows that the technology is required to grow from a handful of existing large-scale projects today to around 3,000 projects by 2050, to secure the above-mentioned 19% share in emission reductions. However, it is worth noting that CCS is not considered as the only policy for establishing an environmentally sustainable growth path, as the development of renewable energy sources are also given a prominent role.<sup>6</sup> Thus, it appears that the recommended mitigation portfolio is a very balanced one.

Without doubt, these studies have been very useful in informing both policymakers and the general public about the available options and costs involved when directing emissions to a more sustainable trajectory. At the same time, however, the welfare economic trade-offs underlying the results are not always transparent, i.e., it is not always clear to what extent differences in scenarios are the result of differences in the constraints imposed (emission caps, technological, and economic constraints) or the differences in trade-offs for which the models allow (e.g., between economic growth and environmental quality).

In this paper, we wish to assess the scope for CCS and CCS R&D as part of a socially efficient solution to the climate change problem. The vehicle that we use for this purpose is the intertemporal model of climate and directed technical change developed by Acemoglu, Aghion, Bursztyn and Hémous (2012, AABH hereafter). In this model, final good production requires two inputs, renewable and fossil fuel energy. Both types of energy are produced using labor and capital with the help of the

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<sup>6</sup>IPCC (2012) reports on 164 commissioned medium- and long-term scenarios from 16 global energy-economic and integrated assessment models. The scenarios range from baseline simulations with CO<sub>2</sub> atmospheric concentrations as high as 1050 ppm by 2100 to those with CO<sub>2</sub> caps as tight as 350 ppm by 2100. The results show that the share of renewable energy varies from today's share of 17% to shares as high as 77% in 2050. But even in some of the baseline scenarios with no CO<sub>2</sub> caps imposed, renewable energy shares can be much higher than those currently, reflecting significant differences regarding the assumptions on the evolution of the energy and abatement technologies (including CCS), energy demand, and prospective fossil fuel availability.

latest available technologies. These technologies result from costly R&D efforts, and given a finite number of scientists, faster technological progress in one sector needs to be balanced against slower progress in the other sector. The production of fossil fuel energy increases the stock of CO<sub>2</sub> in the atmosphere, and therefore contributes to a global increase in temperature. This global warming in turn reduces the quality of the environment and with it the welfare of the representative consumer.

To this model, we append a new sector, that for CCS, which also operates using labor and capital. Like both energy sectors, the CCS technology may be improved by devoting resources to R&D. We calibrate our model using both data on world energy production levels and estimates of the marginal cost of CCS. We then ask ourselves the following questions: (i) is it socially optimal to include CCS in today's or the near future's mitigation portfolio?; and (ii) is it socially optimal to devote R&D resources to improve CCS technology, such that it becomes part of an optimal mitigation policy in the more distant future? We find that given today's marginal costs of CCS and clean and dirty energy production, the answer to both questions is rather bleak. We then ask by how much the marginal cost of CCS needs to fall such that both CCS and R&D into the CCS technology become socially optimal. Surprisingly, we find that the decrease in the cost of CCS must be quite large, at least 56% of the average current estimates.

The remainder of the paper is structured as follows. Section 2 reviews the related literature. Section 3 details the model. In Section 4, we present the details about the numerical implementation. Section 5 provides our main results based on the cost of CCS in total production. In Section 7 we discuss the sensitivity of our results to the level of the maximal concentration of atmospheric CO<sub>2</sub>, and different probabilities of successful research. Section 8 concludes.

## 2 Related literature

In recent years, a literature has developed that studies the desirability of CCS as part of the first-best or second-best environmental policy portfolio used in combating climate change. This literature has developed in several directions: partial *vs* general equilibrium models, theoretical models *vs* numerical solutions to empirically calibrated models, models encompassing exogenous *vs* endogenous technical progress.

An early contribution to this literature is by Goulder and Mathai (2000) who develop a partial equilibrium model to answer the question about how the endogenization of technological progress affects the optimal trajectories for abatement activity and carbon taxes. They show both analytically and through numerical simulations that endogenous technical progress with respect to (w.r.t) abatement activity (what they term "induced technical change" or the possibility of reducing the cost of abatement through devoting resources to R&D) in general lowers the time profile of optimal carbon taxes, and shifts at least some abatement activity from the present to the future.

However, the more recent literature has often taken a general equilibrium approach. We can discern at least two separate strands in this literature. One is concerned with the characterization of socially efficient environmental policy, and its implementation in a decentralized economy, possibly under some second-best policy restrictions (such as upper bounds on the tax rate set on carbon emissions). Examples include Grimaud and Rouge (2014) and Ayong Le Kama et al. (2013). The other strand compares the welfare costs of different (portfolios of) policy instruments when CO<sub>2</sub> stabilization or maximum temperature change targets are imposed. Examples include Gerlagh and van der Zwaan (2006), Grimaud et al. (2011), and Kalkuhl et al. (2015).<sup>7</sup>

Gerlagh and van der Zwaan (2006) use a top-down computable general equilibrium model with an environment module to which they append a CCS sector. Technical progress in this sector stems from learning-by-doing. Assuming a marginal cost of abatement of \$45/ton CO<sub>2</sub> avoided, they compute the carbon emission trajectories for 30 five-year periods (2000–2150) under five stabilization targets (ranging from 450 to 550 ppm–particles per million) and five policy scenarios in addition to a business-as-usual scenario. Their results reveal that irrespective of the stabilization target, subsidization of renewable energy use is the most expensive policy, while a carbon emission tax in which revenue is recycled as a subsidy for non-fossil energy use represents the least costly policy mix. A carbon tax also dominates a policy that charges for fossil fuel use because it incentivizes the use of CCS activity. While CCS activity is low to begin with, about 30–50% of new fossil fuel capacity from 2050 onwards is complemented with CCS equipment.

Grimaud et al. (2011) extend the Goulder and Mathai (2000) framework to a general equilibrium setting. They model a decentralized market economy where energy, capital, and labor are combined into a final good. Energy is produced from non-renewable fuels and a renewable energy source. Growth is endogenous and depends on R&D investments used to promote the efficiency of use of energy in final good production, the efficiency of producing renewable energy, or the efficiency of CCS in reducing the emissions resulting from the use of fossil fuels. In this market economy, investors are able to capture only a fraction of R&D returns and this motivates the use of (differentiated) R&D subsidies. Assuming a cap on atmospheric carbon concentration (450 or 550 ppm), they then provide a general characterization of the second-best trajectory for the tax on carbon emissions and the three R&D subsidies that maximize social welfare. In particular, the carbon tax is shown to follow an inverted U-shaped trajectory. Their main finding is that both tax and subsidy instruments should be used simultaneously to provide the strongest impact, and that R&D in CCS is warranted in the medium term only if accompanied by the imposition of a ceiling on the stock of atmospheric CO<sub>2</sub>.

Grimaud and Rouge (2014) also adopt a general equilibrium approach. In their model, endogenous growth is restricted to the final goods industry. Final output makes use of intermediate goods (embodying technology), labor, and the extracted amounts of a non-renewable energy resource. The

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<sup>7</sup>Preceding this literature one can find studies on pollution-augmenting technical change (i.e., new knowledge allowing production with less pollution and more efficient use of renewable resources) such as Bovenberg and Smulders (1995, 1996). There, the efficiency with which a polluting activity (use of a renewable natural resource/environment) contributes to the production of goods and services is endogenized through costly R&D.

use of energy in production causes emissions that can be abated (i.e., captured and stored) using labor. With a constant and inelastic labor supply, the main trade-off in their model is between output production and abatement. The authors first characterize the socially optimal trajectories with and without access to a CCS technology, and then trace out the paths for a decentralized economy when only second-best policy tools are available. They find that the greatest abatement effort should take place in the near future, and thereafter gradually decline over time. Moreover, compared with an economy without CCS technology, the availability of CCS speeds up the optimal extraction rate and lowers output growth as labor is diverted from R&D activities.

Finally, in a static multi-market general equilibrium model for Europe, Golombek et al. (2011) look at the development of CCS in relation to technology-neutral abatement policies (i.e., carbon taxes or tradable permits)<sup>8</sup>. When an uniform tax of \$90/tCO<sub>2</sub> is implemented, the results show that new coal power plants with CCS become profitable, totally replace non-CCS coal power investments, and partially replace new wind and biomass power plants. For the same tax level, new gas power plants with CCS become profitable and replace almost all non-CCS power investments. Compared to a business-as-usual scenario, this leads to a 90% lower CO<sub>2</sub> emissions in 2030. The results also imply that from a social point of view it is not desirable to retrofit CCS into the existing coal and gas power plants.

Our model shares several aspects with the models described. We employ a global and dynamic general equilibrium setting with four sectors: a “dirty” fossil fuel energy sector, a “clean” renewable energy sector, a CCS sector, and a sector transforming clean and dirty energy into a final good that is used for consumption and capital investment. In addition to the standard labor balance constraint, the economy is endowed with a stock of scientists who can be allocated to each of the three lower-level sectors (clean, dirty, and CCS) where their efforts result in efficiency-enhancing innovations. Moreover, rather than imposing exogenous stabilization targets, we let the quality of the environment enter consumer welfare (cf. Tahvonen and Kuuluvainen (1991), Bovenberg and Smulders (1995) and Grimaud and Rouge (2014)). We are primarily interested in whether CCS activity and CCS-related R&D effort are part of a first-best policy. We characterize the socially optimal solution, proceed by a numerical calibration of our model in the same vein as AABH, and then optimize as in Gerlagh and van der Zwaan (2006) over a finite but long discrete horizon (thirty 10-year periods). Unlike the models reviewed above, we find little scope for (R&D on) CCS.

### 3 The model

We specify a four-sector general equilibrium model, which augments the three-sector model in AABH with a fourth sector responsible for CCS activity. As we are primarily interested in socially optimal policy, we discard any issues related to the implementation of this policy in a market economy through

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<sup>8</sup>Equilibrium is calculated for exogenously taken non-EU parameter values.

taxes and the subsidization of R&D activities. The interested reader is referred to the AABH article.<sup>9</sup>

An infinitely lived representative consumer cares about a final good ( $c_t$ ) and the quality of the environment ( $F_t$ ) in each period  $t$  of life. The period utility function,  $U(c_t, F_t)$ , satisfies the standard monotonicity and concavity assumptions. The final good is produced by means of two energy carriers: dirty energy ( $Y_{dt}$ ) and clean energy ( $Y_{ct}$ ). The (symmetric) production function is assumed to display a constant elasticity of substitution (CES),  $\varepsilon$ :<sup>10</sup>

$$(1) \quad Y_t = \left( Y_{ct}^{\frac{\varepsilon-1}{\varepsilon}} + Y_{dt}^{\frac{\varepsilon-1}{\varepsilon}} \right)^{\frac{\varepsilon}{\varepsilon-1}}.$$

Each of the two energy types  $j$  ( $j = c, d$ ) is produced using labor ( $L_j$ ), of which there is a unit mass available in each period, and capital (machinery,  $x_j$ ), which is available at constant marginal cost  $\psi$ , and which fully depreciates after one period.<sup>11</sup> The sector production functions are of Cobb–Douglas form, with technology parameter (sectoral stock of knowledge)  $A_j$  ( $j = c, d$ ). The same is true for the CCS sector, which we label with index  $a$  (for abatement). Thus,

$$(2) \quad Y_{jt} = A_{jt}^{1-\alpha} L_{jt}^{1-\alpha} x_{jt}^{\alpha} \quad (j = a, c, d).$$

The stock of knowledge/technology level  $A_{jt}$  in sector  $j$  is assumed to grow at a rate of  $\gamma\eta_j s_{jt}$ , where  $s_j$  is the number of researchers allocated to sector  $j$  ( $j = a, c, d$ ),  $\eta_j$  is the probability that a single researcher is successful in creating an innovation, and  $\gamma$  is the relative increase in knowledge in the case of such an innovation.<sup>12</sup> Subsequently,  $A_j$  evolves according to

$$(3) \quad A_{jt} = (1 + \gamma\eta_j s_{jt}) A_{jt-1}.$$

There is a unit mass of scientists available in each period and the allocation of a scientist to one sector

<sup>9</sup>See Grecker and Heggedal (2012) for a discussion of the robustness of R&D subsidy policies prescribed by the AABH model w.r.t. the assumptions on the length of the patent period.

<sup>10</sup>For a discussion regarding the CES function and the value of the elasticity of substitution between the two energy carriers, we refer the reader to Gerlagh and van der Zwaan (2004). Below, we will follow these authors' suggestion of 3 as a reasonable value for  $\varepsilon$ . This value implies that the isoquants are tangent with the input axes, but at the same time have endpoints at  $y^{\frac{3}{2}}$ . Thus, although the CES specification makes it technically feasible to rely solely on renewable energy, such a solution will not be selected as long as the (social) relative price of fossil fuel energy is finite. Alternatively, one could have recourse to a Variable Elasticity of Substitution specification, as in Gerlagh and Lise (2005). The advantage of such specification is that the substitution elasticity between the two energy carriers falls to 1 if one carrier becomes dominant.

<sup>11</sup>Similar to Golosov et al. (2014), when assuming full depreciation, we have in mind a time period of at least 10 years. In our numerical simulations, a period will constitute 10 years.

<sup>12</sup>Thus, there are constant returns to scale (CRS) in research. However, arguments that may provide deviations from CRS in both directions exist. For instance, “fishing out” problems, where easy inventions occur sooner with little effort whereas larger technological challenges are solved later and require more effort, infer decreasing returns to scale, while positive spillovers between researchers and/or labs suggest increasing returns to scale. See Mattauch et al. (2012) for a variant of the AABH model with technical progress stemming from learning-by-doing.

fully crowds out R&D activity in the other sector/s.<sup>13</sup>

With an activity level  $Y_a$  in the CCS sector, the emissions corresponding to  $Y_a$  units of dirty energy input production are captured and stored. The carbon sink (environmental stock) therefore evolves according to the following equation of motion:

$$(4) \quad S_t = -\xi(Y_{dt-1} - Y_{at-1}) + (1 + \delta)S_{t-1},$$

where  $\xi$  is the rate of CO<sub>2</sub> emissions from dirty energy production and  $\delta$  is the regeneration rate of the environment.<sup>14</sup> The size of the carbon sink translates into an environmental quality index  $\tilde{F}(S_t)$  (see p. 12).

As we are primarily interested in optimal policy, we consider the levels of the labor and capital inputs, the level of energy production, the level of CCS activity, and the allocation of scientists that maximize the intertemporal utility of the representative consumer subject to the technology constraints, the equation of motion for the environment and for the sectoral stocks of knowledge, and the

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<sup>13</sup>Pottier et al. (2014) criticize the AABH model for the assumption of an exogenously given number of scientists. Nevertheless, AABH and our model builds on the recent literature on endogenous technical change (see Acemoglu, 2002, 2003). In this regard, the assumption that researchers are scarce, and thus, there is full crowding out of R&D, is standard in this literature. As the number of researchers is constant, economic growth cannot be sustained by increasing the amount of these factors. To maintain growth, there is state dependence in the innovation possibilities frontier. In this regard, the spillovers from previously accumulated knowledge in one sector make researchers in that sector more productive over time. Furthermore, we assume that the aggregate innovation production function has constant returns to accumulated knowledge in the model. This is because if the returns to the accumulated knowledge are slightly higher, the model generates explosive growth. On the other hand, if there are decreasing returns to the accumulated knowledge, productivity growth gradually ceases. The assumption that the number of researchers is constant also allows us to avoid any scale effect on output growth (Jones et al., 1999; Groth, 2007). For example, if the number of researchers was subject to exponential growth, the growth rate of the output in our model would itself grow exponentially.

<sup>14</sup>With a natural upper bound on the environmental stock corresponding to the pre-industrial level of CO<sub>2</sub> in the atmosphere ( $\bar{S}$ ), the equation of motion becomes:  $S_t = \max\{\bar{S}, -\xi(Y_{dt-1} - Y_{at-1}) + (1 + \delta)S_{t-1}\}$ . Absent emission activity, the upper bound would be approached at a constant natural growth rate  $\delta$ . Alternatively, environmental quality could be assumed to grow at a rate depending positively on the discrepancy between  $\bar{S}$  and  $S_t$ , viz.  $S_t - S_{t-1} = \sigma(\bar{S} - S_{t-1}) - \xi(Y_{dt-1} - Y_{at-1})$ . Absent emissions, the gap between  $S_t$  and  $\bar{S}$  narrows down at a decreasing rate and converges to zero asymptotically. See, e.g., Bovenberg and Smulders (1995, 1996). In our simulations, the upper bound is never effective. Hence, we ignore it in the remainder of this section.



balance constraints for labor and scientists:

$$\begin{aligned}
& \max_{\{Y_t, Y_{jt}, L_{jt}, x_{jt}, A_{jt}, s_{jt}\}_{t=0, \dots, \infty}^{j=c, d, a}} \sum_{t=0}^{\infty} \beta^t U(Y_t - \psi(x_{ct} + x_{dt} + x_{at}), \tilde{F}(S_t)) \\
& \text{s.t } Y_t = \left( Y_{ct}^{\frac{\epsilon-1}{\epsilon}} + Y_{dt}^{\frac{\epsilon-1}{\epsilon}} \right)^{\frac{\epsilon}{\epsilon-1}} (\pi_t) \\
& Y_{jt} = A_{jt}^{1-\alpha} L_{jt}^{1-\alpha} x_{jt}^{\alpha} \quad (\pi_{jt}) \quad (j = a, c, d) \\
& A_{jt} = (1 + \gamma \eta_j s_{jt}) A_{jt-1} \quad (\mu_{jt}) \quad (j = a, c, d) \\
& S_t = -\xi(Y_{dt-1} - Y_{at-1}) + (1 + \delta)S_{t-1} \quad (\omega_t) \\
& 1 \geq L_{ct} + L_{dt} + L_{at} \quad (w_t) \\
& 1 \geq s_{ct} + s_{dt} + s_{at} \quad (v_t) \\
& Y_{at} \leq Y_{dt} \quad (\phi_t).
\end{aligned}$$

In this problem,  $\beta$  is the discount factor,  $\psi$  is the amount of final goods necessary to build a machine, and the Lagrange multipliers in brackets following the constraints are all current values (thus the net present value of a marginal unit of labor in period  $t$  is  $\beta^t w_t$ ). The final inequality precludes the more than 100% capture of CO<sub>2</sub> emissions (we ignore the fact that existing CCS technology does not allow for capture rates exceeding approximately 90%). In a market economy, these decisions can be decentralized by means of a tax on the dirty energy input production, subsidies to research on clean energy production and CCS technology, subsidies to machine use (to correct for possible market power of machine producers), and lump-sum transfers to the representative consumer.

In the sequel, we define the social price of sector  $j$  output as  $\hat{p}_{jt} \stackrel{\text{def}}{=} \frac{\pi_{jt}}{\pi_t}$  ( $j = c, d, a$ ), and the *ad valorem* rate on fossil fuel energy use as  $\tau_t \stackrel{\text{def}}{=} \xi \beta \frac{\omega_{t+1}}{\pi_t} \frac{1}{\hat{p}_{dt}}$ . The latter is the social marginal environmental damage of period  $t$  emissions  $\beta \xi \frac{\omega_{t+1}}{\pi_t}$ , expressed as a fraction of the social price of dirty energy,  $\hat{p}_{dt}$ . Thus,  $\tau_t \hat{p}_{dt}$  is the tax per unit of the dirty production. Here,  $\omega_{t+1}$ , the shadow value of the environment at time  $t + 1$ , is the discounted intertemporal sum of marginal disutilities caused by the current dirty input production, which is adjusted for the value of the dirty input and regeneration in every period:

$$\omega_t = \sum_{k=0}^{\infty} \beta^k (1 + \delta)^k U_{F_k} \tilde{F}'_k.$$

In the remainder of this section, we focus on characterizing the optimal policy w.r.t. the CCS sector, in both its level of activity and the efforts directed to R&D. We relegate the solution of the full model to Appendix A.

For both energy carriers, the marginal product in final good production should equal the social price:  $MP_{ct} = \hat{p}_{ct}$  and  $MP_{dt} = (1 + \tau_t) \hat{p}_{dt}$ . For abatement activity (i.e., CCS), the optimality

condition is

$$\hat{p}_{at} \geq \tau_t \hat{p}_{dt} - \frac{\phi_t}{\pi_t},$$

with equality whenever  $Y_{at} > 0$ . The second term on the right-hand side (RHS) is the period  $t$  social cost of not being able to capture more CO<sub>2</sub> than the amount emitted by the dirty sector in period  $t$ ; this cost is obviously zero when  $Y_{at} < Y_{dt}$ . Thus, when  $\hat{p}_{at} > \tau_t \hat{p}_{dt}$ , any abatement is suboptimal. If partial abatement is optimal, then  $\hat{p}_{at} = \tau_t \hat{p}_{dt}$ , while full abatement requires that  $\hat{p}_{at} \leq \tau_t \hat{p}_{dt}$ .

In Appendix A, we show that allocating a scientist to the R&D department of sector  $j$  yields a marginal social value of

$$(5) \quad \frac{\mu_{jt}}{\pi_t} \gamma \eta_j A_{jt-1} = \frac{1}{\pi_t} \frac{\gamma \eta_j}{1 + \gamma \eta_j s_{jt}} (1 - \alpha) \sum_{k=0}^{\infty} \beta^k \pi_{t+k} \hat{p}_{jt+k} Y_{jt+k}.$$

This value positively depends on (i) the productivity of R&D ( $\gamma \eta_j$ ) and (ii) the discounted social value of the output stream ( $\hat{p}_{jt+k} Y_{jt+k}$ ,  $k = 0, 1, \dots, \infty$ ) of sector  $j$ . If R&D in sector  $j$  is optimal, then this marginal social value should match the social wage of the scientists,  $\frac{v_t}{\pi_t}$ . If (5) falls short of  $\frac{v_t}{\pi_t}$ , then R&D is not optimal in sector  $j$ . It is therefore clear from (5) that substantial CO<sub>2</sub> capture and storage in the near future is a prerequisite for justifying R&D in the CCS sector.<sup>15</sup>

The allocation of labor and capital across sectors should satisfy the standard conditions of equality between the marginal products and the corresponding social prices. In Appendix A, we show how the first-order conditions together with the constraints allow us to reduce the above maximization problem to a simpler model in terms of four sets of decision variables:  $\{Y_{at}, \tau_t, s_{ct}, s_{dt}\}_{t=0,1,\dots,\infty}$ . This problem is then calibrated and solved (with MATLAB) for a large but finite time horizon. In the next section, we explain how the calibration is done. The optimal solutions are presented in Section 5 and discussed in Section 6

## 4 Numerical implementation of the model

To implement the model numerically, we proceed as in AABH. We consider a long but finite horizon (300 years) and let a single period consist of 10 years.<sup>16</sup> The base period ( $t = 0$ ) is 1997–2006. The final period ( $T = 30$ ) is 2297–2306.

<sup>15</sup>In a decentralized equilibrium, this would translate into a high price and/or market size effect for CCS.

<sup>16</sup>AABH take a period to be five years. Because our model has two extra sequences of decision variables ( $Y_{at}$  and  $s_{at}$ ,  $t = 1 \dots 300$ ), we double the number of years per period to keep the total number of decision variables in the numerical optimization within limits.

We fix  $\alpha$  to  $\frac{1}{3}$  and  $\varepsilon$  to 3.<sup>17</sup> We then calibrate the model by assuming that in period 0 (the base period) there is no environmental policy. Under this assumption, and using the values for world primary energy production by carrier ( $Y_{d0}$  and  $Y_{c0}$ ), we solve for the base period technology efficiency parameters  $A_{d0}$  and  $A_{c0}$ , as well as their weighted average  $B_0 \stackrel{\text{def}}{=} \left( A_{c0}^{-\varphi} + A_{d0}^{-\varphi} \right)^{-\frac{1}{\varphi}}$  (with  $\varphi \stackrel{\text{def}}{=} (1 - \varepsilon)(1 - \alpha) = -\frac{4}{3}$ ) (see Appendix B):  $A_{d0} = 2658$ ,  $A_{c0} = 1072$ , and  $B_0 = 3232$ . Then, using the result that  $MC_{j0} = \hat{p}_{jt} = \left( \frac{B_0}{A_{j0}} \right)^{1-\alpha}$  (cf. Eq. (23) in Appendix A.), where  $MC_{j0}$  is the social marginal cost of sector  $j$  output, we obtain

$$MC_{d0} = 1.14 \frac{\text{UON}}{\text{QBTU}} \text{ and } MC_{c0} = 2.09 \frac{\text{UON}}{\text{QBTU}},$$

where UON stands for *units of the numeraire* and QBTU are quadrillions ( $10^{15}$ ) of British Thermal Units.

There exists a variety of estimates for the average cost of CCS, each surrounded by a wide confidence interval. In a detailed comparative study, Finkenrath (2011) averages the estimates for the relative increase in levelised cost of electricity for four CO<sub>2</sub> capture methods: post combustion CO<sub>2</sub> capture from coal-fired power generation using amines (63%), pre-combustion CO<sub>2</sub> capture from integrated gasification combined cycles (39%), oxy-combustion CO<sub>2</sub> capture from pulverised coal power generation (64%), and post-combustion CO<sub>2</sub> capture from natural gas combined cycles (33%).<sup>18</sup> We will therefore assume a reference mark-up of 60% but carry out a sensitivity analysis across a wide range around this number. Hence, the reference cost of abating CO<sub>2</sub> when producing one QBTU of dirty energy is

$$MC_{a0} = 1.14 \times .60 \frac{\text{UON}}{\text{QBTU}} = .684 \frac{\text{UON}}{\text{QBTU}}.$$

Having found  $MC_{a0}$ , we calibrate  $A_{a0}$  using the relationship  $MC_a = \left( \frac{B_0}{A_{a0}} \right)^{1-\alpha}$  (cf. (23) in the Appendix A):

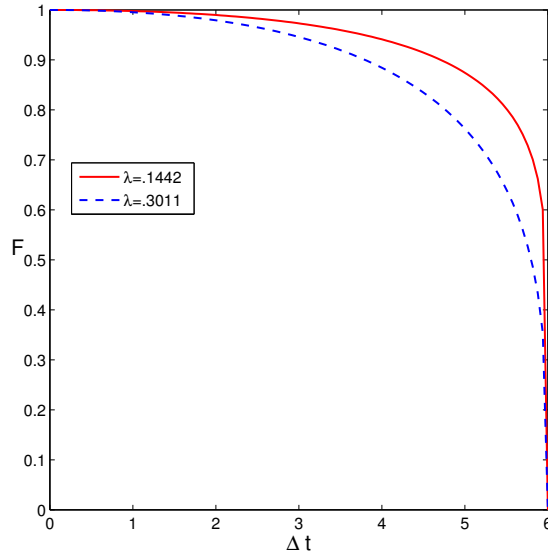
$$A_{a0} = \frac{B_0}{(.684)^{\frac{3}{2}}} = 5713.$$

The quality of the environment,  $\tilde{F}(S_t)$ , is modelled as a decreasing and concave function of the rise in temperature since pre-industrial times:  $\tilde{F}(S_t) = F(\Delta t(S_t))$ , where

$$F(\Delta t) = \frac{(\Delta t_{dis} - \Delta t)^\lambda - \lambda \Delta t_{dis}^{\lambda-1} (\Delta t_{dis} - \Delta t)}{(1 - \lambda) \Delta t_{dis}^\lambda}.$$

<sup>17</sup>The first assumption ensures that the wage bill in a laissez faire economy is  $\frac{2}{3}$  of GDP. For a CES technology, the implied conditional own elasticity for the dirty energy input factor is given by  $\varepsilon$  times the cost share of clean energy factor. With  $\varepsilon = 3$  (AABH, van der Zwaan et al. (2002) and Gerlagh and van der Zwaan (2004)), the implied equilibrium prices for both energy factors (to be computed below) result in a 'clean' cost share of .23. This means that the conditional own elasticity for dirty energy is about  $-.69$ , which is a reasonable value. In a recent study, Papageorgiou et al. (2013) estimate the elasticity of substitution between clean and dirty energy between 1.7 and 2.8 for the electricity sector and between 1.4 and 3.2 for the non-energy sector (panel of cross-country sectoral data).

<sup>18</sup>These mark-ups correspond to the following estimates for the cost of CO<sub>2</sub> avoided: 58, 43, 52, and 80 USD<sub>2010</sub> per ton CO<sub>2</sub>. See the last columns of Tables 3, 5, 7, and 9 in Finkenrath (2011).



**Figure 1:** Damage Function

Here,  $\Delta t_{dis}$  is the increase in temperature leading to environmental disaster. Thus  $F(\Delta t)$  is an index of environmental quality with  $\lambda$  measuring the sensitivity to the temperature increase; it has the properties that  $F(0) = 1$  and  $F(\Delta t_{dis}) = 0$ . For  $\Delta t_{dis} = 6^\circ\text{C}$  and  $\lambda = 0.1442$  (see AABH), the function is depicted as the solid line in the Figure 1. A  $\lambda$ -value of .1442 amounts to a 1% reduction in environmental quality following a  $2^\circ\text{C}$  global temperature increase. But we will also consider a more pessimistic scenario with  $\lambda$ -value of .3011; this produces 2% damage at the same temperature increase (cf. Weitzman (2010); see the dashed line in Figure 1).

The rise in temperature is a decreasing function of the carbon sink in the atmosphere,  $S_t$ :

$$\Delta t = 3 \log\left(\frac{280 \times 2^{\frac{\Delta t_{dis}}{3}} - S_t}{280}\right) / \log(2),$$

where 280 refers to the atmospheric concentration of  $\text{CO}_2$ , measured in ppm (particles per million by volume) since pre-industrial times.

World  $\text{CO}_2$  emissions from energy consumption during the base period were 272040 ( $2 \times 136020$ ) million tons (EIA (2008), Table 11.19). As  $Y_{d0} = 3786 (= 2 \times 1893)$  QBTU, this means an emission rate of

$$\frac{272040 \text{ million ton CO}_2}{3786 \text{ QBTU}} = 71.85 \frac{\text{million ton CO}_2}{\text{QBTU}}.$$

As 7.78 billion tons of emitted  $\text{CO}_2$  give rise to an increase in atmospheric concentration of  $\text{CO}_2$  of one ppm, the emission rate as ppm per QBTU is

$$\xi = 71.85 \frac{\text{million ton CO}_2}{\text{QBTU}} \times \frac{1}{7.78 \frac{\text{billion ton CO}_2}{\text{ppm}}} = .0092 \frac{\text{ppm}}{\text{QBTU}}.$$

$S_0$ , the environmental quality in the base period, is set at 741 ppm,<sup>19</sup> and  $\delta$ , the regeneration rate of the environment, is set at 50% of emissions in the base period, i.e.,  $\delta = \frac{1}{2} \frac{\text{emissions}_0}{S_0} = .0236$  ( $= 2 \times .0118$ ) (cf. AABH, 2012). The utility function is assumed to take the Cobb–Douglas (CD) form  $U(c, F) = \frac{[c \cdot F]^{1-\sigma}}{1-\sigma}$ , with  $\sigma = 2$ . However, because the use of this particular utility function has been criticized for allowing too easy substitution of consumption for environmental quality (Weitzman, 2010), we also ran simulations using a CES utility function with a substitution elasticity of  $\frac{1}{2}$  (cf. Sterner and Persson (2008)):  $U(c, F) = \frac{1}{1-\sigma} \left( \frac{1}{2} c^{\frac{\theta-1}{\theta}} + \frac{1}{2} F^{\frac{\theta-1}{\theta}} \right)^{\frac{\theta}{\theta-1} (1-\sigma)}$  with  $\sigma = 2$  and  $\theta = \frac{1}{2}$ . As we show below, this does not change the qualitative nature of our results (cf. Figure 5 below).

Finally, we follow AABH by assuming a discount rate of 0.015 (so that  $\beta = .9852$ ). The technological progress parameters are chosen as follows:  $\gamma = 1$ , and  $\eta \equiv \eta_c = \eta_d = \eta_a = .2$  per 10-year period (i.e., 2% per year, cf Jones, 2015, Table 2).

Following the numerical simulations, we carry out sensitivity analyses. First, we consider disaster level of temperature rise of 4°C and 3°C, which correspond to maximal concentrations of atmospheric CO<sub>2</sub> of 700ppm and 550ppm, respectively, that need to be avoided. Second, we allow for a 3% per year probability of successful research in the renewable energy and CCS sectors (the "infant" sectors) for the first 50 years. This concludes the calibration of our model.

## 5 Main Results

We first present the results for  $MC_a = .684$  (recall that this corresponds to a mark-up of 60% for the levelized cost of "dirty" electricity and to a cost of 58\$/tCO<sub>2</sub> avoided) when preferences are of CD form and  $\lambda = .1442$ . The results are presented in Figure 2. Panel b shows the time path for the optimal tax rate  $\tau_t$  as well as the cost of CCS relative to the marginal cost of dirty energy. Since  $MC_{at}/MC_{dt}$  ( $= \hat{p}_{at}/\hat{p}_{dt}$ ) always exceeds  $\tau_t$ , it is never optimal to have capture and storage of CO<sub>2</sub> emissions (panel d). Because CCS is never active, there are no scientists allocated to CCS R&D (panel a). Note that the initial R&D activity on "dirty" energy carriers increases the cost of CCS relative to that of  $Y_d$ . These trajectories are identical to those depicted in Figure 1 in AABH. In particular, after about 50 years, scientists are relocated from the dirty energy sector in favor of the clean energy sector. Together with the tax on dirty energy, the result is a gradual increase in the intensity of clean energy in final good production (panel e). The temperature continues to increase but stabilizes below the disaster level of a temperature rise of 6°C. If  $\lambda$  is increased to 0.3011, although deteriorating the environmental impact of a (smaller-than-disaster-level) temperature rise, the overall picture remains

<sup>19</sup>Initial environmental quality is calculated as the difference between  $\bar{S}$ , that is, the environmental quality that corresponds to the pre-industrial level of CO<sub>2</sub> in the atmosphere, and the CO<sub>2</sub> level in the base period (379 ppm),

$$S_0 = 2^{\frac{\Delta t_{dis}}{3}} 280 - 379.$$

Thus for  $\Delta t_{dis} = 6$ ,  $S_0 = 1120 - 379 = 741$ .

almost the same, except that the switch from “clean” to “dirty” R&D takes place a few years earlier. The result is a slightly lower temperature increase to which the climate converges.

–Figure 2a-f here–

As the current estimates for the marginal cost of CCS make neither CCS nor R&D on CCS part of the optimal policy portfolio, we ask by how much this marginal cost must fall before CCS and/or R&D on CCS start to be desirable. When  $MC_a = .55$  (corresponding to a mark-up of 48%), CCS becomes optimal 200 years later. The reason is the steady increase in the tax rate on  $Y_d$ , passing the relative cost of abatement around  $t = 220$ . From then on, CCS becomes active, but not for long as the use of the dirty input becomes quite minimal. See Figure 3 for details. However, in line with our explanation following Eq. (5), the fact that CCS is only active in the distant future makes it suboptimal to divert any R&D resources to that sector in the near future. We categorize these scenarios—without any R&D on CCS, but possibly with active CCS in the distant future—under *Regime 1*. Our simulations show that Regime 1 continues to hold for  $MC_a$  values as low as 0.31 (corresponding to a mark-up of 27%)—see the dashed lines in Figure 4.<sup>20</sup>

–Figure 3a-f here–

For lower  $MC_a$  values, a second regime, *Regime 2*, becomes optimal. This is shown in Figure 4 by the solid lines, which show the optimal policy for  $MC_a = .30$ . ( $MC_a = .30$  corresponds to a mark-up of 26% for the levelized cost of “dirty” electricity and to a cost of 25\$/tCO<sub>2</sub> avoided.) In this regime, CCS becomes active after 50 years, i.e., sooner than in Regime 1, and fossil fuel energy generation without CCS phases out almost entirely in 140 years (see panel d). The second difference w.r.t. Regime 1 is that R&D in CCS now becomes part of the optimal research policy (see panel a). Whereas in Regime 1 only clean R&D prevails in the distant future, there is no role at all for “clean” R&D in Regime 2. Conversely, “dirty” R&D dominates for about 100 years, after which the scientists are shared about equally with the CCS sector.

–Figure 4a-f here–

In Figure 5 we have plotted the maximal intertemporal welfare against values for  $MC_{a0}$ . Recall that  $MC_{a0} = .684(.25)$  corresponds to a mark-up of 60%(22%) over  $MC_{d0}$ . The maximal value function is drawn for the scenario described above (CD preferences,  $\lambda = .1442$ ) but also for the case of CES preferences and  $\lambda = .3011$ . For all scenarios, we discern the same pattern: Regime 1 for modest to high CCS marginal cost values and Regime 2 for very low values.

–Figure 5a-b here–

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<sup>20</sup>At  $MC_a = .31$ , CCS becomes active after 70 years and activity increases to as high as 100% around  $t = 220$ , after which it begins to decline. These high CCS rates do not necessarily imply a growth in the absolute amounts captured and stored. The reason is the diminishing use of the dirty energy carriers in Regime 1, as shown in the lower left panel of the figure.

The switch from Regime 1 to Regime 2 when  $MC_a$  drops below some critical value in [.30, .31] points to a non-convexity in the model owing to the endogenous nature of the R&D activity. We will elaborate on this in the next section.

## 6 Discussion

Before moving to the sensitivity analysis, it is useful to interpret the results obtained so far. The main objectives of the planner is to secure long-run consumption growth and a sustainable quality of the environment. The latter objective can be achieved either through an extensive use of renewable energy or by capturing the CO<sub>2</sub> emissions from fossil fuel energy production. The first alternative is initially about 14.6% more expensive than the second. Consumption growth depends on output growth, which, in turn, depends on overall productivity growth. The overall productivity index for the economy is a weighted average of the efficiency parameters  $A_j$  ( $j = c, d, a$ ). In Appendix A, Eq. (22), we show that this index is given by

$$B_t \stackrel{\text{def}}{=} \left( A_{ct}^{-\varphi} + A_{dt}^{-\varphi} \left[ 1 + \min \left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} \right]^{1-\varepsilon} \right)^{-\frac{1}{\varphi}}.$$

In order to sketch a clear picture, let us abstract from situations with partial abatement. In Regime 1, when CCS is absent, and thus,  $\tau_t < (A_{dt}/A_{at})^{1-\alpha}$ , the productivity index simplifies to

$$(6) \quad B_t = \left( A_{ct}^{-\varphi} + A_{dt}^{-\varphi} [1 + \tau_t]^{1-\varepsilon} \right)^{-\frac{1}{\varphi}}.$$

We can think of the RHS as a CES overall productivity function with the sectoral efficiencies as inputs. This function has a (constant) elasticity of substitution equal to  $1/(1 + \varphi)$ , which turns negative for a large elasticity of substitution in production. Indeed, with  $\varepsilon = 3$  and  $\alpha = 1/3$ ,  $1/(1 + \varphi) = -3$ . Therefore, the isoquants in the  $(A_c, A_d)$ -space are concave w.r.t. the origin. This means that one should either spur clean R&D or dirty R&D, but not both. Replacing  $A_{jt}$  with  $A_{jt-1}(1 + \gamma\eta s_{jt})$  turns Eq. (6) into an overall knowledge production function defined over the R&D resources. Since the period resource constraint,  $s_{ct} + s_{dt} = 1$ , is symmetric, the choice of one corner solution over the other depends on the inherited relative efficiency,  $(A_{dt-1}/A_{ct-1})^{-\varphi}$ , and the tax term  $(1 + \tau_t)^{1-\varepsilon}$ . A large inherited efficiency will favour the allocation of all scientists to the dirty energy sector. But as  $\varepsilon > 1$ , a sufficiently high tax rate will incite the reallocation of all scientists to the clean sector. The initial advantage of dirty energy production then explains why a steep hike in the tax rate is required to move the economy in *Regime 1* from a dirty to a clean R&D focus. This also explains the "scissor"-shape in the upper-left panels of Figures 2-4. Another implication of Eq. (6) is then that in the long run, the productivity index Eq. (6) will grow at the same rate as  $A_c$  does, i.e.,  $\gamma\eta$ .

In Regime 2, when there is full abatement, and therefore,  $\tau_t \geq (A_{dt}/A_{at})^{1-\alpha}$ , the overall produc-

tivity index can be written as

$$(7) \quad B_t = \left( A_{ct}^{-\varphi} + \left[ \left( A_{dt}^{-(1-\alpha)} + A_{at}^{-(1-\alpha)} \right)^{-\frac{1}{1-\alpha}} \right]^{-\varphi} \right)^{-\frac{1}{\varphi}}.$$

The RHS is now a two-level CES function over the three efficiency parameters  $A_{jt}$  ( $j = c, d, a$ ). At the lower level (square bracket term), the stocks of knowledge in the dirty energy and CCS sectors are aggregated into a productivity index for fully abated fossil fuel energy. This function has an elasticity of substitution equal to  $1/(2 - \alpha)$ , which amounts to  $3/5$  when  $\alpha = 1/3$ . Therefore, efficiency in the production of dirty energy and abatement are strong complements, implying that research resources devoted to the dirty sector, should be allocated about evenly to the enhancement of both  $A_d$  and  $A_a$ . This explains the ">"-shape in the upper left panel of Figure 4. The higher level CES function is defined on the efficiency for renewable energy production and fully abated fossil energy generation. Like in the no-abatement case, this function has an elasticity of substitution equal to  $1/(1 + \varphi)$  which is negative for the selected coefficient values. This explains why we do not observe a scenario where researchers are shared between all three sectors. In the long run, the productivity index given by Eq. (7) will grow at a weighted average of the growth rates of  $A_d$  and  $A_a$ . Since researchers are shared evenly among these two sector,  $B$  and, therefore, output and consumption grow only at the rate  $\gamma\eta/2$ . This also transpires from the lower right panel in Figure 4: around year 180, both consumption paths cross, after which the dashed path (Regime 1) increases twice as fast as the solid one (Regime 2).

Figure 4 also reveals that Regime 1, compared to Regime 2, favors the environment in the medium run ( $50 < t < 130$ ) but performs worse in terms of consumption for  $t \in [50, 180]$ . The trade-off then becomes apparent. In Regime 1, the development and use of renewable energy technology favours the environment in the medium run at the cost of a lower consumption level. In Regime 2, the gradual use and development of CSS technology allows for a higher consumption level in the medium run at the cost of higher temperature rise. For  $MC_a$  around .3, both strategies are equally good in terms of discounted utility. The fact that the clean strategy allows for a sustainable long run growth rate that is twice as large is probably unimportant in this respect: with an annual discount rate of 1.5%, the long run ( $t > 180$ ) is given very little weight.

We can sum up these findings as follows. First, the large elasticity of substitution between clean and dirty energy induces a negative elasticity of substitution between the productivities of the clean sector and dirty sector (possibly complemented with CCS) in the determination of the economy's overall productivity index. This means that the allocation of R&D resources is characterized by corner solutions and that changes in the nature of the solution only come about by large changes in policy and/or cost parameters. Second, the clean strategy allows for a long run growth rate that is twice as large, but gives a lower consumption profile in the medium run, in favour of a smaller increase in temperature. This suggests two things. The first is that a lower discount rate will favor Regime 1 since this regime sustains a long-run growth rate that is twice as high. This is also what we find:



taking  $\rho = .001$ , Regime 1 dominates Regime 2 for  $MC_a$  as low as .1. Second, Regime 1 will also be superior when more weight is given to the environment. This is conformed when we perform a sensitivity analysis w.r.t. the disaster temperature.

## 7 Sensitivity Analysis

In all of the above scenarios, the temperature increases above the critical value of  $2^\circ\text{C}$ , and one may wonder whether penalizing temperature rises more heavily could “rescue” CCS as a viable environmental policy instrument. For this reason, we also ran the model under the assumption that environmental disasters are caused by  $3^\circ\text{C}$  or  $4^\circ\text{C}$  rises in the temperature. It turns out that the implications of lower  $\Delta t_{dis}$  values are substantial decreases in CCS activity and resources dedicated to its R&D in case of Regime 2, or, even, the disappearance of this regime altogether. For example, when  $MC_a = .30$ , Regime 2 became optimal under the  $\Delta t_{dis} = 6^\circ$  scenario, but it no longer does when a disaster occurs with a  $4^\circ\text{C}$  increase in temperature (see Figure 6). Rather, the solution is Regime 1, with resources now devoted sooner to the renewable energy R&D (panel a). Moreover, the CCS sector, which once became active after 50 years in Regime 2, now becomes operative only after 130 years and is short-lived owing to the strongly declining use of dirty energy carriers. Another implication is a lower optimal trajectory for the tax rate on  $Y_d$ , which is an outcome of a strong bias towards non-fossil fuel energy use and the earlier devotion of resources to related R&D activities.

–Figure 6a-f here–

When  $\Delta t_{dis} = 3^\circ\text{C}$ , all scientific activity is diverted to the clean sector after 10 years. See Figure 7 (panel a). The share of fossil fuels in the energy mix contracts more sharply and the CCS sector becomes completely idle from the start (see panels d and e). An earlier switch to clean R&D and non-fossil fuel carriers results in an even lesser rise in the global temperature ( $2^\circ\text{C}$ ) and lower optimal tax trajectory (panel b).

–Figure 7a-f here–

One may object to the assumption that all three sectors share the same rate of success in innovation. In comparison to mature technologies, technologies that are in their early stages of development may be expected to display higher rates of successful research. To test the implications of such a differentiation, we assumed that the rate of success in innovation in the renewable energy and CCS sectors exceeds temporarily (50 years) the rate in the fossil energy sector with 1% ( $\eta_c = \eta_a = .03$  and  $\eta_d = .02$  per annum). Figure 8 shows the results for the ‘critical’  $MC_a$  value of .30. Compared with Figure 4, we see that Regime 2 is replaced by Regime 1: even though research on CCS technology is potentially more successful, the facts that CCS activity is complementary to the dirty energy production and the latter cannot grow at the same rate reduce the scope for CCS. As a consequence, it becomes optimal to fully allocate the researchers to the clean sector in the long run (despite a short

reallocation after 50 years, when all three research sectors face the same potential rate of successful innovation again).

–Figure 8a-f here–

## 8 Conclusion

In recent decades, carbon capture and storage has been considered as a promising strategy to curb CO<sub>2</sub> emissions and therefore to address the problem of global warming. Given the infancy of CCS technology, and the need for further research, development and demonstration, it is desirable to assess the optimality of this strategy not only on the basis of its current marginal cost, but also on the potential for improvements in cost efficiencies following R&D efforts in dirty energy, clean energy, and CCS sectors.

For this purpose, we utilized the directed technical change model of Acemoglu et al. (2012) by adding a sector responsible for CCS. Assuming that CCS competes for the same R&D resources as the fossil fuel and renewable energy sectors, and that neither sector has any comparative advantage in transforming R&D into technological improvements, we have computed the Pareto-efficient time paths for production and research activity in each sector.

Surprisingly, we found that even for very optimistic estimates for the current marginal cost of CCS (\$58/tCO<sub>2</sub>), it is not optimal in either the near or the distant future to deploy this abatement technology and dedicate research efforts to it. It is only when we consider current marginal costs less than about 50% of the optimistic reference level, that a regime with CCS and R&D of CCS technology becomes optimal, but even then not in the near future. We also observed that a more stringent environmental constraint (in the form of lower disaster temperature rise) limited the scope for the CCS sector and the corresponding R&D activity.

The stylized model we worked with can be extended in several directions. One dimension is related to the dirty energy carrier, which we assumed to be constrained by the amount of labor and capital devoted to transforming it into energy. Accordingly, we could have introduced a finite fossil fuel resource. However, as CCS depends on fossil fuel use, this will increase neither the scope for CCS nor the R&D devoted to this technology. Similarly, less favourable conditions for CCS (such as technically feasible capture rates below 100%, limited storage possibilities, and the risk of CO<sub>2</sub> leakage), while making the model more realistic, would only reduce the scope for this form of abatement activity and its technology. Conversely, in our model renewable energy is being produced under rather optimistic circumstances, as we have assumed away any problems of intermittency and related problems regarding energy storage. An interesting avenue for future research would, therefore, be to evaluate the scope for CCS when such favorable conditions are absent.

One can also conjecture that if one energy carrier is or becomes dominant, the ease of substitution

with alternative carriers would be reduced. This suggests an inverse-U-shaped relationship between the intensity of, say, fossil fuels, and the elasticity of substitution between fossil fuels and renewable energy (cf. footnote 10 and Gerlagh and Lise (2005, pp. 249)). As it will become more difficult to substitute away from dirty energy when this carrier is dominant, we expect that this would favour the role for CCS in our model. The exploration of these issues is left for future research.

In our paper, we have confined ourselves to a search for the first-best policies. With a sufficiently broad set of instruments, these policies should be decentralizable even in imperfect market economies. Accordingly, two market imperfections will need to be addressed: a tax on dirty production and subsidies to research activities because of R&D externalities.<sup>21</sup> In particular, targeting the right technologies to subsidize is a difficult task (Greaker and Heggedal, 2012) and can lead to misdirection of resources. As this will lead to deviations from the optimal policy, a more aggressive tax policy can be called for to direct technical change and in turn avoid a climate disaster. A heavier use of carbon tax will lead to a higher demand for CCS and, indeed, can attract more researchers to improve the CCS technology. This will have interesting implications and will be crucial when linking the CCS technology better with actual policies.

Lastly, Hoel and Jensen (2012) show that if policy makers can at best commit to a future climate policy while failing to agree on adoption of a current policy, the reaction of fossil fuel owners (to advance the extraction of fossil fuels in time) may make it more desirable to aim at a faster technical progress in abatement rather than in renewable energy production. The consequences of such restrictions for our model would be worthwhile investigating.

## APPENDICES

### A Solution of the model

The Lagrangian function for the planning problem is:

$$\mathcal{L} = \sum_{t=0}^{\infty} \beta^t W_t,$$

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<sup>21</sup>In Acemoglu et al. (2012) machines are supplied by monopolistically competitive firms. In this case there is a third market imperfection. Therefore, machine users will need to be subsidized.

where

$$\begin{aligned}
W_t &= U(Y_t - \psi \sum_{j=a,c,d} x_{jt}, \tilde{F}(S_t)) \\
&+ \pi_t \left[ \left( Y_{ct}^{\frac{\epsilon-1}{\epsilon}} + Y_{dt}^{\frac{\epsilon-1}{\epsilon}} \right)^{\frac{\epsilon}{\epsilon-1}} - Y_t \right] + \sum_{j=a,c,d} \pi_{jt} \left[ L_{jt}^{1-\alpha} A_{jt}^{1-\alpha} x_{jt}^\alpha - Y_{jt} \right] \\
&+ w_t \left[ 1 - \sum_{j=a,c,d} L_{jt} \right] + v_t \left[ 1 - \sum_{j=a,c,d} s_{jt} \right] + \sum_{j=a,c,d} \mu_{jt} \left[ (1 + \gamma \eta_j s_{jt}) A_{jt-1} - A_{jt} \right] \\
&+ \omega_t \left[ -\xi (Y_{dt-1} - Y_{at-1}) + (1 + \delta) S_{t-1} - S_t \right] + \phi_t [Y_{dt} - Y_{at}].
\end{aligned}$$

Thus  $W_t$  is the undiscounted period  $t$  welfare,  $\pi_t$  is the social value of final production in period  $t$ ,  $w_t(v_t)$  is the shadow value of labor (research) in period  $t$ ,  $\mu_{jt}$  is the social value of productivity in sector  $j$  in period  $t$ , and  $\omega_t$  is the social value of the environment in period  $t$ . When writing the quality index of the environment as a function of the stock of CO<sub>2</sub>, we have subsumed the relationship through the increase in temperature,  $\Delta t$ .

The first-order condition (FOC) w.r.t.  $Y_t$  shows that  $\pi_t = U_{ct}$ . The FOC w.r.t.  $S_t$  shows that  $U_{F_t} \tilde{F}'_t = \omega_t - (1 + \delta)\beta\omega_{t+1}$ . This is a forward-looking equation that can be solved for  $\omega_t$ , the social value of a one unit improvement of the environment in  $t$ , as:

$$\omega_t = \sum_{k=0}^{\infty} \beta^k (1 + \delta)^k U_{F_k} \tilde{F}'_k.$$

Improving the environment today thus generates a stream of future benefits.

We now solve for the remaining decision variables. First, note that because of the CES specification, both the clean and dirty inputs will be used in strictly positive quantities. For the clean input, we obtain the optimality condition:

$$MP_{ct} = \hat{p}_{ct} \stackrel{\text{def}}{=} \frac{\pi_{ct}}{\pi_t},$$

i.e., the equality of its marginal product,  $MP_{ct}$ , with its social price. A similar condition holds for the dirty input, corrected for the environmental externality:

$$(8) \quad MP_{dt} = \hat{p}_{dt} + \xi \beta \frac{\omega_{t+1}}{\pi_t} - \frac{\phi_t}{\pi_t},$$

where  $\hat{p}_{dt} \stackrel{\text{def}}{=} \frac{\pi_{dt}}{\pi_t}$ , the social price of the dirty input. The term  $\xi \beta \frac{\omega_{t+1}}{\pi_t}$  is equivalent to a tax on the use of the dirty input in a decentralized solution. It ensures a more moderate use of the dirty input than the equality of  $MP_{dt}$  with  $\hat{p}_{dt}$  would call for. The extra term  $\frac{\phi_t}{\pi_t}$  is due to abatement. Before

interpreting it, we give the FOC w.r.t.  $Y_{at}$ :

$$-\pi_{at} + \xi\beta\omega_{t+1} - \phi_t \leq 0,$$

with equality when  $Y_{at} > 0$ . Dividing through by  $\pi_t$  and defining  $\widehat{p}_{at} \stackrel{\text{def}}{=} \frac{\pi_{at}}{\pi_t}$ , we can write this as:

$$\widehat{p}_{at} \geq \xi\beta\frac{\omega_{t+1}}{\pi_t} - \frac{\phi_t}{\pi_t}.$$

If any abatement is suboptimal,  $Y_{at} = 0 < Y_{dt}$ , and  $\widehat{p}_{at} \geq \xi\beta\frac{\omega_{t+1}}{\pi_t}$ ; the social marginal cost of abatement is too high compared with its social marginal benefit. However, suppose that abatement is optimal, then either there is partial abatement,  $0 < Y_{at} \leq Y_{dt}$ , in which case  $\widehat{p}_{at} = \xi\beta\frac{\omega_{t+1}}{\pi_t}$ , or there is full abatement,  $Y_{at} = Y_{dt}$ , in which case  $\widehat{p}_{at} \leq \xi\beta\frac{\omega_{t+1}}{\pi_t}$ . In this last case, the social marginal benefit is larger than the social marginal cost, but the welfare programme is constrained by the fact that abatement can only apply to contemporaneous emissions, not to CO<sub>2</sub> emitted in previous periods (i.e., it is not possible to remove previously emitted CO<sub>2</sub> from the atmosphere). If this is the case, then social welfare may be increased by expanding dirty input production beyond the level where  $MP_{dt} = \widehat{p}_{dt} + \xi\beta\frac{\omega_{t+1}}{\pi_t}$ . Indeed, then:

$$(9) \quad MP_{dt} = \widehat{p}_{dt} + \widehat{p}_{at}.$$

CO<sub>2</sub> abatement is merely an additional social cost. Thus, we can conclude that:

$$(10) \quad MP_{dt} = \widehat{p}_{dt} + \min\{\widehat{p}_{at}, \xi\beta\frac{\omega_{t+1}}{\pi_t}\},$$

$$(11) \quad = \widehat{p}_{dt} + \min\{\widehat{p}_{at}, \tau_t\widehat{p}_{dt}\}.$$

Having determined the optimality conditions for  $Y_{jt}$ , we now consider the use of labor and physical capital. Both inputs are required in positive amounts. For labor, the value of the marginal product of labor in the production of sector  $j$  must equal the social wage rate  $\widehat{w}_t \stackrel{\text{def}}{=} \frac{w_t}{\pi_t}$ :

$$(12) \quad \widehat{p}_{jt}MP_{Ljt} = \widehat{w}_t, \text{ or}$$

$$(13) \quad (1 - \alpha)\widehat{p}_{jt}A_{jt}^{1-\alpha} \left(\frac{x_{jt}}{L_{jt}}\right)^\alpha = \widehat{w}_t.$$

Likewise, for machines:

$$(14) \quad \widehat{p}_{jt}MP_{xjt} = \psi, \text{ or}$$

$$(15) \quad \alpha\widehat{p}_{jt}A_{jt}^{1-\alpha} \left(\frac{L_{jt}}{x_{jt}}\right)^{1-\alpha} = \psi,$$

where  $\psi$  is the (exogenously given) amount of final goods necessary to build one machine.

Finally, we determine the allocation of scientists, and the production of knowledge. The FOC w.r.t.  $s_{jt}$  is:

$$\frac{\mu_{jt}}{\pi_t} \gamma \eta_j A_{jt-1} \leq \hat{v}_t \stackrel{\text{def}}{=} \frac{v_t}{\pi_t},$$

with equality whenever  $s_{jt} > 0$ . The left-hand side (LHS) is the social price of sector  $j$  knowledge,  $\frac{\mu_{jt}}{\pi_t}$ , times the marginal knowledge production of an additional researcher. The RHS is the social wage rate of a researcher.

The final set of FOCs characterizes the allocation of productivity improvements in the different sectors across time. The FOC w.r.t.  $A_{jt}$  reads:

$$\hat{p}_{jt}(1 - \alpha) L_{jt}^{1-\alpha} \left( \frac{x_{jt}}{A_{jt}} \right)^\alpha = \frac{\mu_{jt}}{\pi_t} - \beta \frac{\mu_{jt+1}}{\pi_{t+1}} \frac{\pi_{t+1}}{\pi_t} (1 + \gamma \eta_j s_{jt+1}).$$

The LHS is the value of the marginal product of newly acquired knowledge on the use of machines. Using (15), an optimal allocation of knowledge implies that the social price of sector  $j$  knowledge,  $\frac{\mu_{jt}}{\pi_t}$ , must evolve according to the rule:

$$(1 - \alpha) \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} L_{jt} \hat{p}_{jt}^{\frac{1}{1-\alpha}} = \frac{\mu_{jt}}{\pi_t} - \beta \frac{\mu_{jt+1}}{\pi_{t+1}} \frac{\pi_{t+1}}{\pi_t} (1 + \gamma \eta_j s_{jt+1}).$$

Multiplying through by  $\pi_t A_{jt}$  and making use of  $A_{jt+1} = (1 + \gamma \eta_j s_{jt}) A_{jt}$  give:

$$\mu_{jt} A_{jt} = (1 - \alpha) \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} L_{jt} \pi_t \hat{p}_{jt}^{\frac{1}{1-\alpha}} A_{jt} + \beta \mu_{jt+1} A_{jt+1}.$$

The social value of acquired knowledge in sector  $j$  at time  $t$  is the value of  $A_{jt}$  priced at its marginal product plus the “standing on the shoulder of giants” effect (future knowledge builds on today’s knowledge). Using the forward operator  $F$ , multiplying through by  $\gamma \eta_j \frac{A_{jt-1}}{A_{jt}}$  and making use of  $A_{jt} = (1 + \gamma \eta_j s_{jt+1}) A_{jt-1}$  result in:

$$\begin{aligned} (16) \quad \frac{\mu_{jt}}{\pi_t} \gamma \eta_j A_{jt-1} &= \frac{1}{\pi_t} \frac{\gamma \eta_j}{1 + \gamma \eta_j s_{jt+1}} \frac{1}{1 - \beta F} (1 - \alpha) \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} L_{jt} \pi_t \hat{p}_{jt}^{\frac{1}{1-\alpha}} A_{jt}, \\ &= \frac{1}{\pi_t} \frac{\gamma \eta_j}{1 + \gamma \eta_j s_{jt+1}} (1 - \alpha) \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} \sum_{k=0}^{\infty} \beta^k L_{jt+k} \pi_{t+k} \hat{p}_{jt+k}^{\frac{1}{1-\alpha}} A_{jt+k}, \end{aligned}$$

so that the social value of allocating an extra researcher to sector  $j$  is given by the discounted sum of future knowledge levels, appropriately valued and weighted.

Solving (15) for  $x_{jt}$  gives:

$$(17) \quad x_{jt} = \left( \alpha \frac{\widehat{p}_{jt}}{\psi} \right)^{\frac{1}{1-\alpha}} A_{jt} L_{jt},$$

which can be plugged into (13) to yield the social price of sector  $j$  output, as a weighted average of the exogenous machine price,  $\psi$ , and the shadow price of labor,  $\widehat{w}_{jt}$ :

$$(18) \quad \widehat{p}_{jt} = \frac{1}{\mathcal{A}} \frac{1}{A_{jt}^{1-\alpha}} \widehat{w}_t^{1-\alpha} \psi^\alpha,$$

where  $\mathcal{A} \stackrel{\text{def}}{=} \alpha^\alpha (1-\alpha)^{1-\alpha}$ . Hence, at an optimum,  $\widehat{p}_{jt}$  will equal the social marginal cost of sector  $j$  output.

Next, the FOCs for  $Y_{ct}$  and  $Y_{dt}$  can be used to relate these input levels to aggregate output,  $Y_t$  and the shadow prices of the inputs:

$$(19) \quad \begin{aligned} Y_{ct} &= Y_t \widehat{p}_{ct}^{-\varepsilon} \text{ and} \\ Y_{dt} &= Y_t [\widehat{p}_{dt} + \min\{\widehat{p}_{at}, \tau_t \widehat{p}_{dt}\}]^{-\varepsilon} \\ &= Y_t \widehat{p}_{dt}^{-\varepsilon} \left[ 1 + \min\left\{ \frac{\widehat{p}_{at}}{\widehat{p}_{dt}}, \tau_t \right\} \right]^{-\varepsilon} \\ (20) \quad &= Y_t \widehat{p}_{dt}^{-\varepsilon} \left[ 1 + \min\left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} \right]^{-\varepsilon}, \end{aligned}$$

where the last equality follows from (18). Making use of the final good production function, we obtain:

$$1 = \widehat{p}_{ct}^{1-\varepsilon} + \widehat{p}_{dt}^{1-\varepsilon} \left[ 1 + \min\left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} \right]^{1-\varepsilon}.$$

As  $\widehat{p}_{jt}$  ( $j = c, d, a$ ) are given by (18):

$$1 = \frac{1}{\mathcal{A}^{1-\varepsilon}} \widehat{w}_t^\varphi \psi^{\alpha(1-\varepsilon)} \left( A_{ct}^{-\varphi} + A_{dt}^{-\varphi} \left[ 1 + \min\left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} \right]^{1-\varepsilon} \right),$$

where  $\varphi \stackrel{\text{def}}{=} (1-\alpha)(1-\varepsilon)$ .

Hence, we can solve for the social value of the wage rate:

$$(21) \quad \begin{aligned} \widehat{w}_t &= \mathcal{A}^{\frac{1}{1-\alpha}} \psi^{-\frac{\alpha}{1-\alpha}} \left( A_{ct}^{-\varphi} + A_{dt}^{-\varphi} \left[ 1 + \min\left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} \right]^{1-\varepsilon} \right)^{-\frac{1}{\varphi}} \\ &= \mathcal{A}^{\frac{1}{1-\alpha}} \psi^{-\frac{\alpha}{1-\alpha}} B_t, \end{aligned}$$

thereby implicitly defining the “sector average” productivity parameter  $B_t$  as:

$$(22) \quad B_t \stackrel{\text{def}}{=} \left( A_{ct}^{-\varphi} + A_{dt}^{-\varphi} \left[ 1 + \min \left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} \right]^{1-\varepsilon} \right)^{-\frac{1}{\varphi}}.$$

From (21) and (18), the social prices of the two inputs as well as the price of abatement are then:

$$(23) \quad \widehat{p}_{jt} = \left( \frac{B_t}{A_{jt}} \right)^{1-\alpha} \quad (j = c, d, a).$$

Machine use in sector  $j$  can be obtained from (17) and (23):

$$(24) \quad x_{jt} = \widehat{p}_{jt}^{\frac{1}{1-\alpha}} \left( \frac{\alpha}{\psi} \right)^{\frac{1}{1-\alpha}} A_{jt} L_{jt} = \left( \frac{\alpha}{\psi} \right)^{\frac{1}{1-\alpha}} B_t L_{jt},$$

and therefore the aggregate machine cost (the share of final good production used for capital) is:

$$(25) \quad AMC_t \stackrel{\text{def}}{=} \sum_{j=c,d,a} \psi x_{jt} = \psi \left( \frac{\alpha}{\psi} \right)^{\frac{1}{1-\alpha}} B_t \sum_{j=c,d,a} L_{jt} = \psi^{-\frac{\alpha}{1-\alpha}} \alpha^{\frac{1}{1-\alpha}} B_t,$$

where the last equality follows from the normalization of the labor supply to one.

To find the levels of production in the three sectors, we plug the solution for  $x_{jt}$  (24) into the production function, yielding:

$$Y_{jt} = A_{jt} L_{jt} \left( \alpha \frac{\widehat{p}_{jt}}{\psi} \right)^{\frac{\alpha}{1-\alpha}} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} L_{jt} A_{jt}^{1-\alpha} B_t^\alpha \quad (j = c, d, a).$$

Therefore  $L_{jt} = \left( \frac{\alpha}{\psi} \right)^{-\frac{\alpha}{1-\alpha}} A_{jt}^{\alpha-1} B_t^{-\alpha} Y_{jt}$ , which allows us to write (16) as:

$$\begin{aligned} \frac{\mu_{jt}}{\pi_t} \gamma \eta_j A_{jt-1} &= \frac{1}{\pi_t} \frac{\gamma \eta_j}{1 + \gamma \eta_j s_{jt+1}} (1 - \alpha) \sum_{k=0}^{\infty} \beta^k A_{jt+k}^\alpha B_{t+k}^{-\alpha} Y_{jt+k} \pi_{t+k} \widehat{p}_{jt+k}^{\frac{1}{1-\alpha}} \\ &= \frac{1}{\pi_t} \frac{\gamma \eta_j}{1 + \gamma \eta_j s_{jt+1}} (1 - \alpha) \sum_{k=0}^{\infty} \beta^k \pi_{t+k} \widehat{p}_{jt+k} Y_{jt+k}, \end{aligned}$$

where the second equality follows from (23). This is expression (5) in the text.

On the other hand, (19) and (20) together with (23) give:

$$(26) \quad Y_{ct} = Y_t \left( \frac{B_t}{A_{ct}} \right)^{-\varepsilon(1-\alpha)}, \text{ and}$$

$$(27) \quad Y_{dt} = Y_t \left( \frac{B_t}{A_{dt}} \right)^{-\varepsilon(1-\alpha)} \left[ 1 + \min \left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} \right]^{-\varepsilon}.$$



The last three expressions now allow us to write the labor balance equation as:

$$(28) \quad A_{ct}^{-\varphi} B_t^{-(1-\varphi)} Y_t + A_{dt}^{-\varphi} B_t^{-(1-\varphi)} \left[ 1 + \min \left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} \right]^{-\varepsilon} Y_t \\ + Y_{at} A_{at}^{-(1-\alpha)} B_t^{-\alpha} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}}.$$

We now look at the three possibilities. The first is where there is full abatement,  $Y_{at} = Y_{dt}$ , such that  $\min \left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} = \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}$ . In that case:

$$Y_{at} = Y_{dt} = Y_t \left( \frac{B_t}{A_{dt}} \right)^{-\varepsilon(1-\alpha)} \left[ 1 + \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha} \right]^{-\varepsilon}.$$

Making use of these values for  $Y_{at}$  and  $Y_{dt}$  in the labor balance equation (28) reduces the latter to:

$$\left( \frac{\alpha}{\psi} \right)^{-\frac{\alpha}{1-\alpha}} B_t^{-(1-\varphi)} B_t^{-\varphi} Y_t = 1,$$

so that

$$(29) \quad Y_t^{FA} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} B_t, \\ Y_{ct}^{FA} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} B_t^{\varphi+\alpha} A_{ct}^{1-(\varphi+\alpha)}, \\ Y_{dt}^{FA} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} B_t^{\varphi+\alpha} A_{dt}^{1-(\varphi+\alpha)} \left[ 1 + \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha} \right]^{-\varepsilon}, \text{ and} \\ Y_{at}^{FA} = Y_{dt}^{FA}.$$

In the second case, there is partial abatement such that  $0 < Y_{at} < Y_{dt}$  and  $\min \left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} = \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha} = \tau_t$ . Now (28) becomes:

$$\left\{ A_{ct}^{-\varphi} B_t^{-(1-\varphi)} Y_t + A_{dt}^{-\varphi} B_t^{-(1-\varphi)} [1 + \tau_t]^{-\varepsilon} Y_t + Y_{at} A_{at}^{-(1-\alpha)} B_t^{-\alpha} \right\} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}},$$

yielding:

$$(30) \quad Y_t^{PA} = \left\{ \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} - Y_{at} A_{at}^{-(1-\alpha)} B_t^{-\alpha} \right\} \frac{B_t^{1-\varphi}}{\left[ A_{ct}^{-\varphi} + A_{dt}^{-\varphi} [1 + \tau_t]^{-\varepsilon} \right]},$$

$$(31) \quad Y_{ct}^{PA} = Y_t^{PA} \left( \frac{B_t}{A_{ct}} \right)^{-\varepsilon(1-\alpha)},$$

$$(32) \quad Y_{dt}^{PA} = Y_t^{PA} \left( \frac{B_t}{A_{dt}} \right)^{-\varepsilon(1-\alpha)} [1 + \tau_t]^{-\varepsilon}.$$

For this to be compatible with partial abatement, we need  $Y_{at} \leq Y_{dt}^{PA}$ , which can be shown to be equivalent with:

$$(33) \quad Y_{at} \leq \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} \frac{A_{dt}^{\varepsilon(1-\alpha)} B_t^\alpha [1 + \tau_t]^{-\varepsilon}}{\left\{ A_{ct}^{-\varphi} + A_{dt}^{-\varphi} [1 + \tau_t]^{1-\varepsilon} \right\}}.$$

Given partial abatement is optimal, we have  $\left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha} = \tau_t$ , and this condition reduces to:

$$(34) \quad Y_{at} \leq \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} \frac{A_{dt}^{\varepsilon(1-\alpha)} B_t^{1-\varepsilon(1-\alpha)}}{[1 + \tau_t]^\varepsilon}.$$

In the third case, there is no abatement:  $Y_{at} = 0$  and  $\min\left\{ \left( \frac{A_{dt}}{A_{at}} \right)^{1-\alpha}, \tau_t \right\} = \tau_t$ . The equilibrium value for  $Y_t$  is then found by setting  $Y_{at} = 0$  in (30):

$$(35) \quad Y_t^{NA} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} \frac{B_t^{1-\varphi}}{\left[ A_{ct}^{-\varphi} + A_{dt}^{-\varphi} [1 + \tau_t]^{-\varepsilon} \right]},$$

and

$$Y_{ct}^{NA} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} \frac{B_t^\alpha A_{ct}^{\varepsilon(1-\alpha)}}{\left[ A_{ct}^{-\varphi} + A_{dt}^{-\varphi} [1 + \tau_t]^{-\varepsilon} \right]},$$

$$Y_{dt}^{NA} = \left( \frac{\alpha}{\psi} \right)^{\frac{\alpha}{1-\alpha}} \frac{B_t^\alpha A_{dt}^{\varepsilon(1-\alpha)}}{\left[ A_{ct}^{-\varphi} + A_{dt}^{-\varphi} [1 + \tau_t]^{-\varepsilon} \right]} [1 + \tau_t]^{-\varepsilon}, \text{ and}$$

$$Y_{at}^{NA} = 0.$$

When solving the model, we search for a sequence  $\{Y_{at}, \tau_t, s_{ct}, s_{dt}\}_{t=0}^T$  (where  $T$  is large) that

maximizes:

$$\sum_{t=0}^T \beta^t U(Y_t^{PA}(Y_{at}) - AMC_t, \tilde{F}((1 + \delta)S_{t-1} - \xi(Y_{dt-1} - Y_{at-1}))),$$

subject to the equality constraints (25), (31), (32),  $s_{at} = 1 - s_{ct} - s_{dt}$ ,  $A_{jt} = (1 + \gamma\eta_j s_{jt}) A_{jt-1}$  (all  $t$  and  $j$ ), the non-linear inequality constraint (33), the non-negativity constraint  $Y_t^{PA}(Y_{at}) - AMC_t \geq 0$ , and with the initial productivity levels  $A_{j0}$  given.

## B Calibration of the model

Without any policy intervention in the base period, the laissez-faire levels for clean and dirty input production are:

$$Y_{c0} = \left(\frac{\alpha}{\psi}\right)^{\frac{\alpha}{1-\alpha}} \frac{B_0^\alpha A_{c0}^{\varepsilon(1-\alpha)}}{A_{c0}^{-\varphi} + A_{d0}^{-\varphi}}, \text{ and } Y_{d0} = \left(\frac{\alpha}{\psi}\right)^{\frac{\alpha}{1-\alpha}} \frac{B_0^\alpha A_{d0}^{\varepsilon(1-\alpha)}}{A_{c0}^{-\varphi} + A_{d0}^{-\varphi}},$$

where  $B_0 \stackrel{\text{def}}{=} \left(A_{c0}^{-\varphi} + A_{d0}^{-\varphi}\right)^{-\frac{1}{\varphi}}$ , and  $\varphi \stackrel{\text{def}}{=} (1 - \varepsilon)(1 - \alpha)$ . This system can be solved for  $A_{c0}$  and  $A_{d0}$ :

$$\begin{aligned} A_{d0} &= \left(\frac{\alpha}{\psi}\right)^{-\frac{\alpha}{1-\alpha}} Y_{d0} \left[1 + \left(\frac{Y_{d0}}{Y_{c0}}\right)^{\frac{1-\varepsilon}{\varepsilon}}\right]^{\frac{\alpha+\varphi}{\varphi}}, \\ A_{c0} &= \left(\frac{\alpha}{\psi}\right)^{-\frac{\alpha}{1-\alpha}} Y_{c0} \left[1 + \left(\frac{Y_{c0}}{Y_{d0}}\right)^{\frac{1-\varepsilon}{\varepsilon}}\right]^{\frac{\alpha+\varphi}{\varphi}}. \end{aligned}$$

As in AABH, we have used the values for world primary energy production by energy carrier during the period 2002–2006 (EAI (2008), Table 11.1) and doubled them. Dirty carriers (coal, natural gas, crude oil, and natural gas plant liquids) yield 3786 QBTU, while clean carriers (nuclear electric power, hydroelectric power, geothermal, and others) provide 615 QBTU.<sup>22</sup> Under the assumptions that  $\alpha = \frac{1}{3}$ ,  $\varepsilon = 3$  (and therefore  $\varphi = -\frac{4}{3}$ ),  $\rho = 0.015$ , and the normalization  $\psi = \alpha^2$  (Acemoglu et al., 2012), we obtain the following estimates for  $A_{d0}$ ,  $A_{c0}$ , and  $B_0$ :  $A_{d0} = 2658$ ,  $A_{c0} = 1072$ , and  $B_0 = 3232$ .

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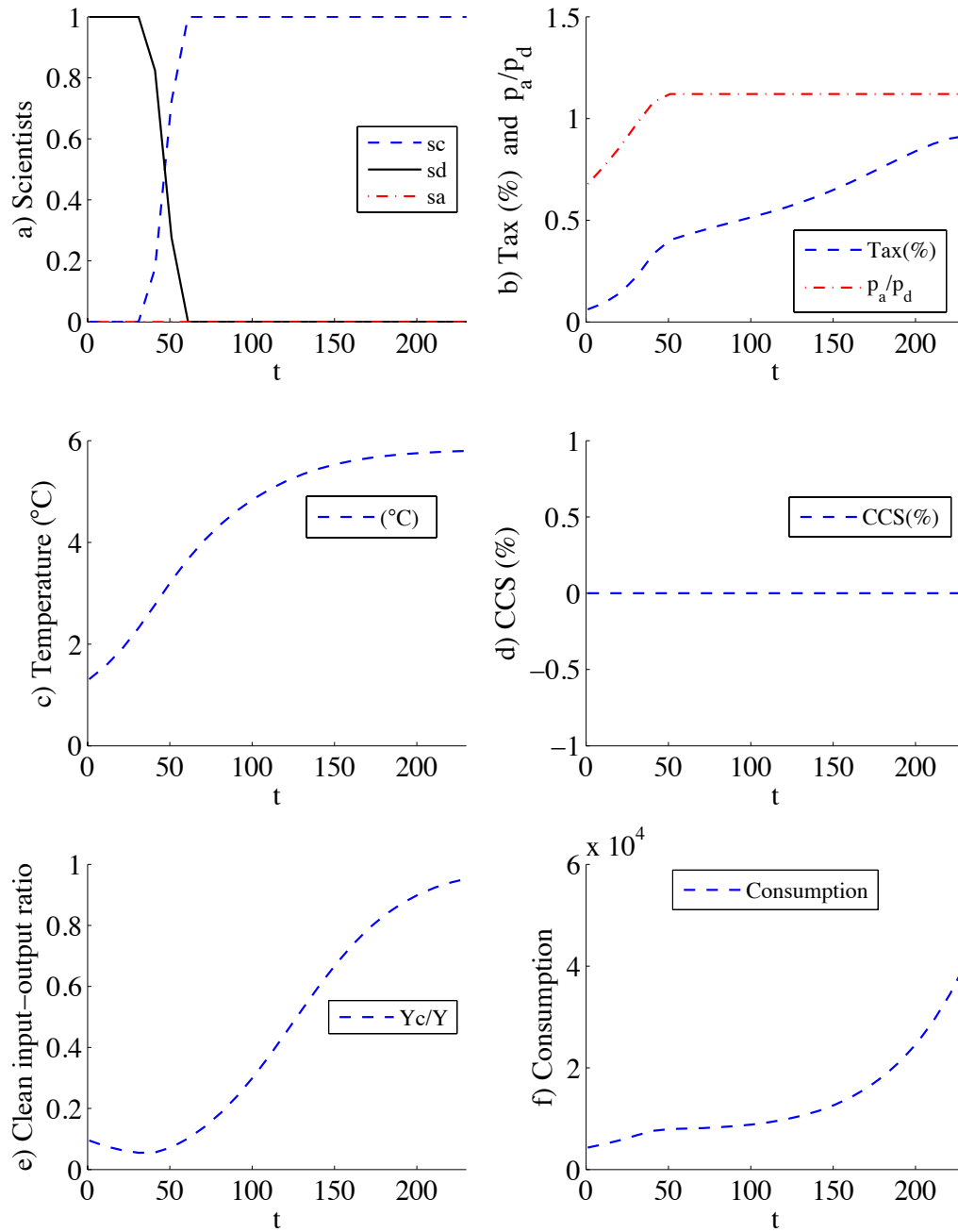
<sup>22</sup>The corresponding values for 2002–2006, adopted by AABH were 1893.25 and 307.77, respectively.

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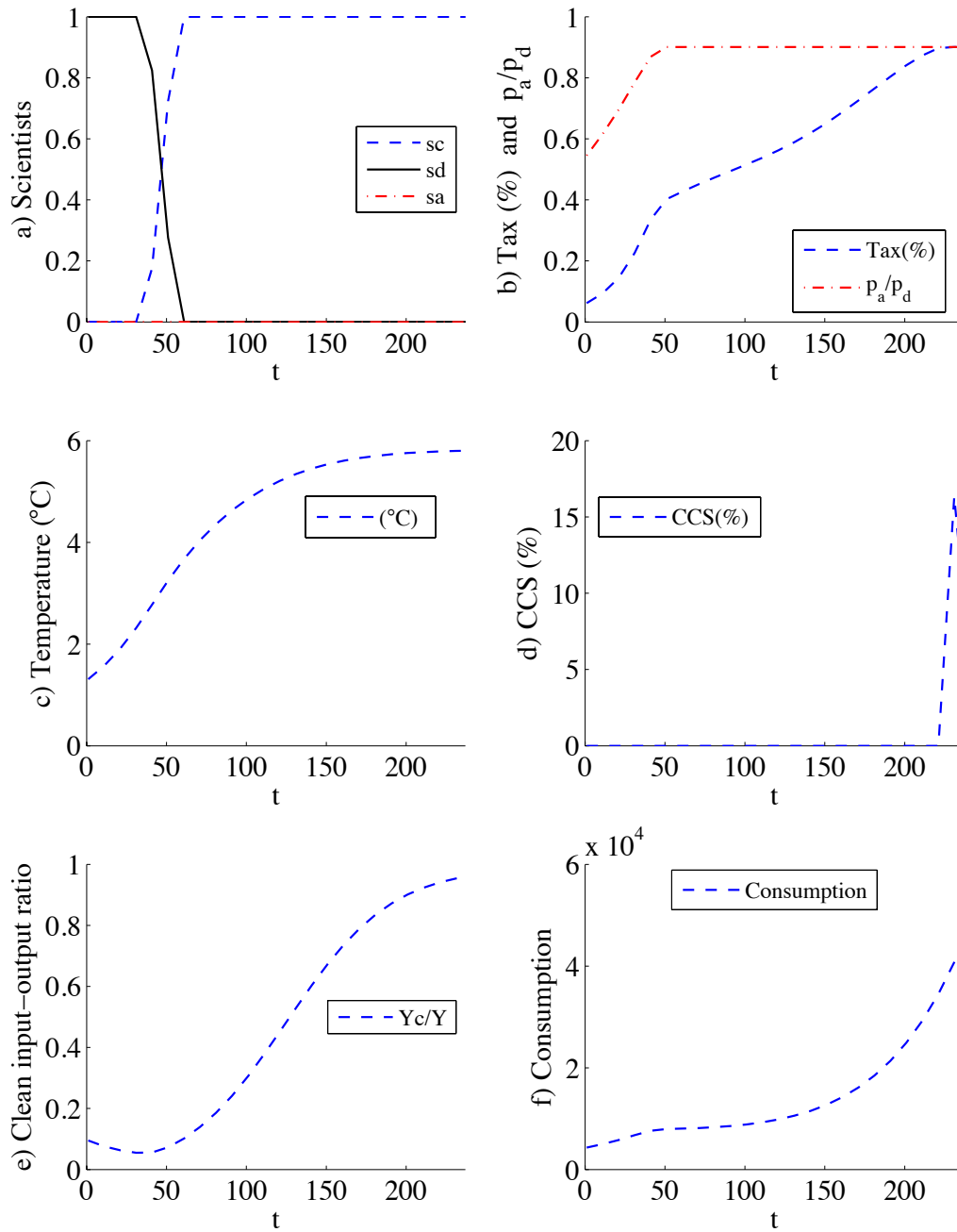
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**Figure 2:** CD preferences,  $\lambda = .1442$ ,  $MC_{a0} = \hat{p}_{a0} = .684$  (60% mark-up over  $MC_{d0}$ ).

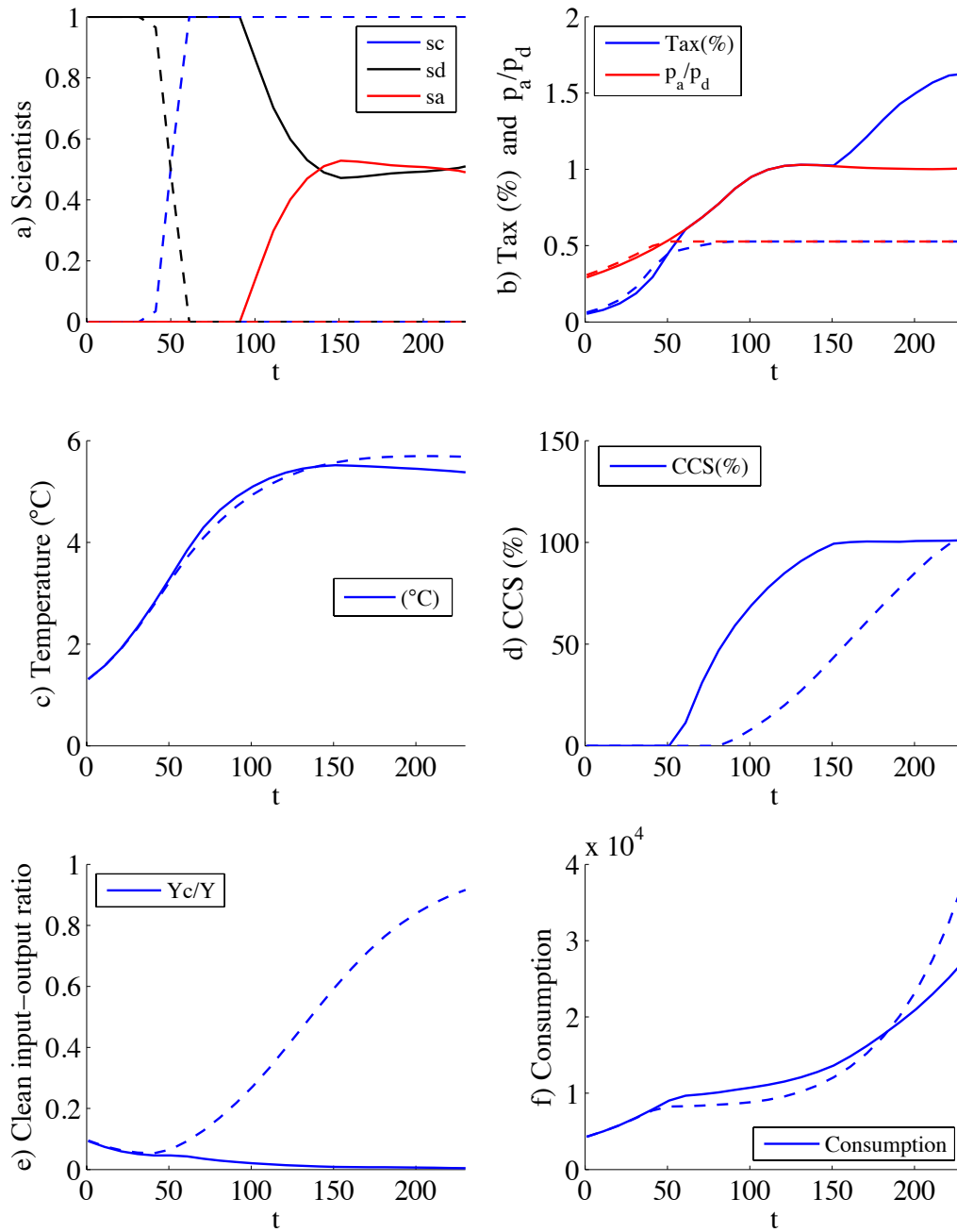


**Figure 3:** CD preferences,  $\lambda = .1442$ ,  $MC_{a0} = .55$  (48% mark-up over  $MC_{d0}$ ).

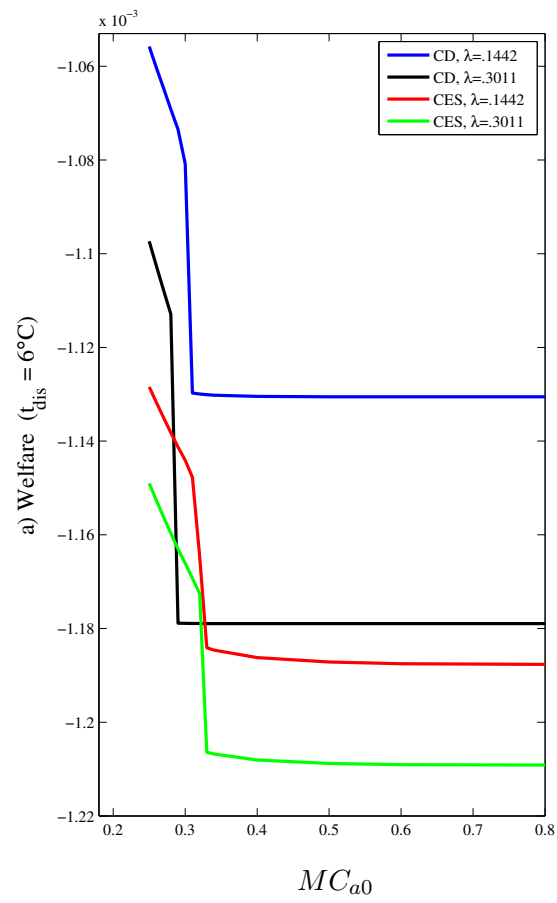




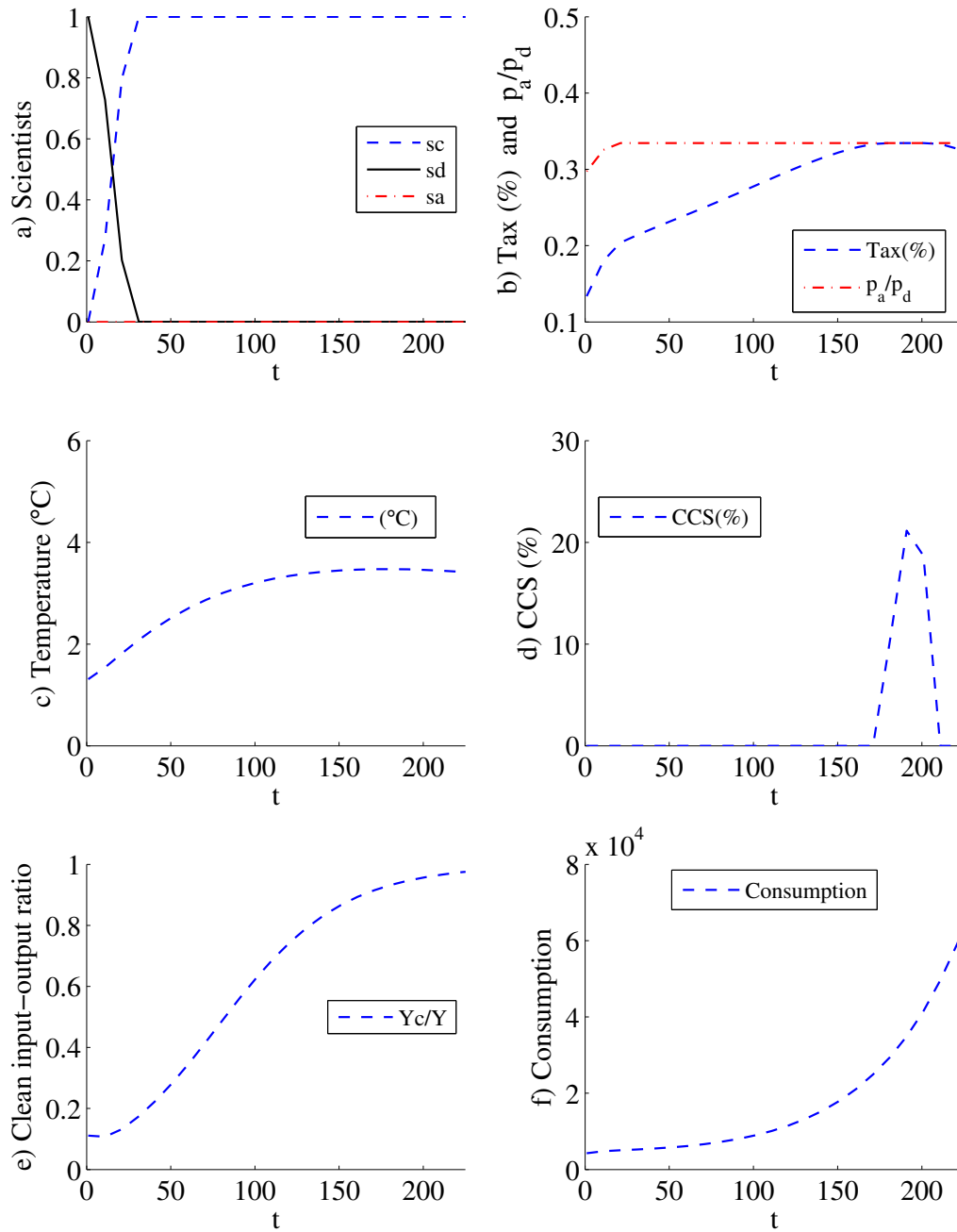
**Figure 4:** CD preferences,  $\lambda = .1442$ ,  $MC_{a0} = .3$  (26% mark-up over  $MC_{d0}$ ).



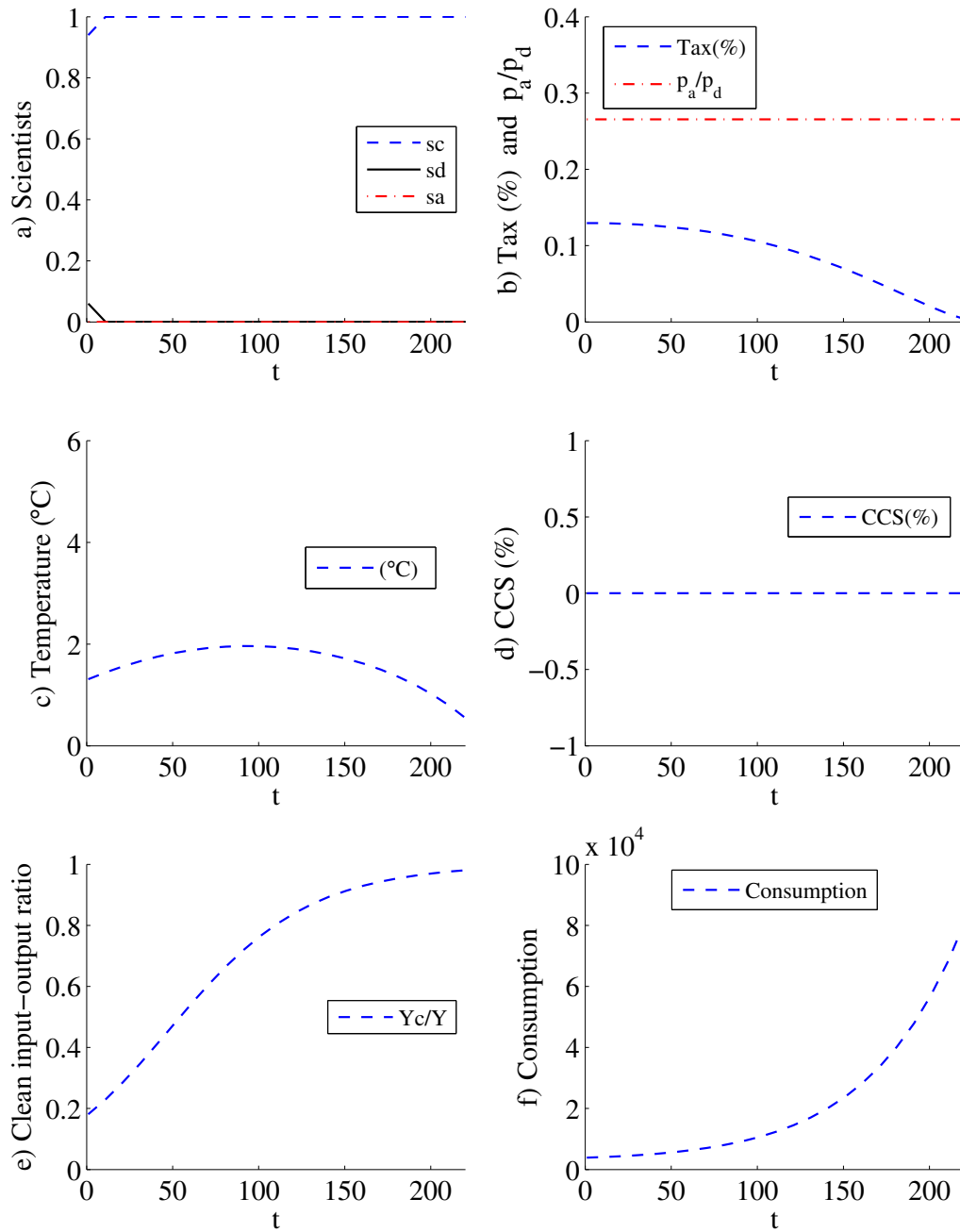
**Figure 5:** Maximal intertemporal welfare levels given  $MC_{a0}$ .



**Figure 6:** CD preferences,  $\lambda = .1442$ ,  $MC_{a0} = .3$ ,  $\Delta t_{dis} = 4^\circ\text{C}$ .



**Figure 7:** CD preferences,  $\lambda = .1442$ ,  $MC_{a0} = .3$ ,  $\Delta t_{dis} = 3^\circ\text{C}$ .



**Figure 8:** CD preferences,  $\lambda = .1442$ ,  $MC_{a0} = .3$ ,  $\eta_c = \eta_a = 0.03$  for the first 50 years, followed by  $\eta_c = \eta_a = 0.02$ .

